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Compositional Semantics  
Heinrich Heine University  
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Room: 25.22-U1.72

## Introduction to Compositional Semantics

### 1 Semantics

Semantics: The study of meaning.

**What is meaning?** Clue: The meanings of the English word *means* all have to do with consequences:

- Epistemic consequences: Smoke means fire (Grice 1957)
- Practical consequences: This means we're going to have to move
- Logical consequences: Being a bachelor means being unmarried

How can you tell whether somebody or something understands? Does Google understand language?

An argument that it does not: Google can't do *inferences*:

- (1) Obama was born in 1961  $\models$  Obama was born in the 1960s
- (2) JFK was assassinated  $\models$  JFK is dead

The left sentences *imply* the right sentences.

The right sentences *follow from* the left sentences.

The right sentences are *consequences* of the left sentences.

The right sentences can be *inferred* from the left sentences.

A hallmark of a system or agent that understands language / grasps meaning is that it can infer the right sentences from the left sentences.

Example of a computer system designed to be able to do inferences: Cyc (Symbolic Artificial Intelligence): Reasoning + commonsense/world knowledge. Recent trend in computer science: Recognizing Textual Entailments.

Doing semantics you can think of yourself as a software engineer, building a machine that is capable of inferring sentences from other sentences.

### **Kinds of inferences:**

1. Entailment (domain of semantics)
2. Presupposition (semantics/pragmatics)
3. Implicature (pragmatics)

In this course, we focus primarily on entailments. What are entailments? Chierchia and McConnell-Ginet (1990) give four alternative definitions for ‘A entails B’:

- Whenever A is true, B is true
- The information that B conveys is contained in the information that A conveys
- A situation describable by A must also be a situation describable by B
- *A and not B* is contradictory (can’t be true in any situation)

To understand why these all mean basically the same thing, we have to understand a little bit of logic.

Logic also helps us understand the view that “To know the meaning of a sentence is to know its truth-conditions” (Heim and Kratzer 1998). What is the relationship between truth conditions and semantic entailment?

## **2 Montague semantics**

*Formal semantics* uses tools from logic to capture the meanings of sentences (primarily entailments, but also presuppositions). It is inspired primarily by the work of Richard Montague, who said:

I reject the contention that an important theoretical difference exists between formal and natural languages. ... In the present paper I shall accordingly present a precise treatment, culminating in a theory of truth, of a formal language that I believe may reasonably be regarded as a fragment of ordinary English. ... The treatment given here will be found to resemble the usual syntax and model theory (or semantics) [due to Tarski] of the predicate calculus, but leans rather heavily on the intuitive aspects of certain recent developments in intensional logic [due to Montague himself]. (Montague 1970b, p.188 in Montague 1974)

What does he mean, syntax and model theory of the predicate calculus?

Predicate calculus is a formal language; a logic. Logics have a syntax and a semantics.

**Syntax:** specifies which formulas of the logic are well-formed.

**Semantics:** specifies which objects (given a model) the formulas correspond to.

Two examples of statements in predicate calculus:

$$\text{LOVE}(\text{JOHN}, \text{MARY})$$

$$\forall x[\text{LOVE}(\text{MARY}, x) \Rightarrow \text{HAPPY}(x)]$$

**Syntactic categories.** Formulas are built up from the following expressions of the following syntactic categories:

- individual constants
- variables
- predicate constants
- logical connectives
- quantifiers

**Semantic types.** Each expression belongs to a certain semantic type. The types of PC are:

- individuals
- relations
- truth values (True or False)

For our examples we have:

Expressions	Syntactic categories	Semantic Type
JOHN, MARY	(individual) constant	individual
$x$	variable	individual
HAPPY	unary predicate constant	unary relation
LOVE	binary predicate constant	binary relation
LOVE(JOHN, MARY)	formula	truth value
HAPPY( $x$ )	formula	truth value
$\forall x[\text{LOVE}(\text{MARY}, x) \Rightarrow \text{HAPPY}(x)]$	formula	truth value

**Montague's idea: English as a formal language.** Montague's idea is to give a semantics for a fragment of English in the same way that we define semantics for formal logics like predicate calculus.

**Example.** Lexical entries:<sup>1</sup>

- $\llbracket \text{Kim} \rrbracket = \text{Kim}$
- $\llbracket \text{run} \rrbracket = \{x \mid x \text{ runs}\}$

<sup>1</sup>Taken from a handout by Chris Kennedy.

- $\llbracket \text{smoke} \rrbracket = \{x \mid x \text{ smokes}\}$
- $\llbracket \text{not} \rrbracket = \text{set complementation}; \llbracket \text{not} \rrbracket(A) = \{x \mid x \notin A\}$
- $\llbracket \text{and} \rrbracket = \text{set intersection}; \llbracket \text{and} \rrbracket(A, B) = \{x \mid x \in A \text{ and } x \in B\}$

### Modes of Composition.

- **Predication**

If  $\alpha$  is a constituent whose immediate subconstituents are  $\beta$  and  $\gamma$ , and if  $\llbracket \beta \rrbracket$  is an individual and  $\llbracket \gamma \rrbracket$  a set of individuals, then  $\llbracket \alpha \rrbracket = 1$  if  $\llbracket \beta \rrbracket \in \llbracket \gamma \rrbracket$  (i.e., if  $\llbracket \beta \rrbracket$  is a member of  $\llbracket \gamma \rrbracket$ ), and 0 otherwise.

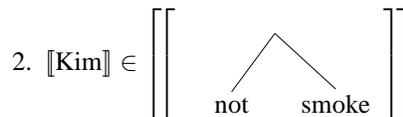
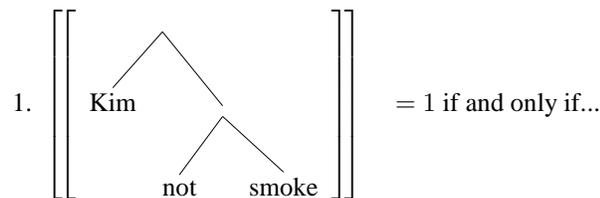
- **1-place application**

If  $\alpha$  is a constituent whose immediate subconstituents are  $\beta$  and  $\gamma$ , and if  $\llbracket \beta \rrbracket$  is a 1-place set-theoretic operation (e.g. set complementation) and  $\llbracket \gamma \rrbracket$  is a set of individuals, then  $\llbracket \alpha \rrbracket = \llbracket \beta \rrbracket(\llbracket \gamma \rrbracket)$ .

- **2-place application**

If  $\alpha$  is a constituent whose immediate subconstituents are  $\beta x$ ,  $\gamma$  and  $\delta$ , and if  $\llbracket \beta \rrbracket$  is a 2-place set-theoretic operation (e.g. set intersection) and  $\llbracket \gamma \rrbracket$  and  $\llbracket \delta \rrbracket$  are sets of individuals, then  $\llbracket \alpha \rrbracket = \llbracket \beta \rrbracket(\llbracket \gamma \rrbracket, \llbracket \delta \rrbracket)$ . ( $\llbracket \alpha \rrbracket$  is the result return by applying  $\llbracket \beta \rrbracket$  to the pair  $\llbracket \gamma \rrbracket, \llbracket \delta \rrbracket$ .)

### Computing truth conditions



**[Predication]**

3.  $\llbracket \text{Kim} \rrbracket \in \llbracket \text{not} \rrbracket(\llbracket \text{smoke} \rrbracket)$

**[1-pl app.]**

4.  $\llbracket \text{Kim} \rrbracket \in \{x \mid x \notin \llbracket \text{smoke} \rrbracket\}$

5.  $\llbracket \text{Kim} \rrbracket \in \{x \mid x \notin \{y \mid y \text{ smokes}\}\}$

6.  $\llbracket \text{Kim} \rrbracket \notin \{x \mid x \text{ smokes}\}$