

## Homework 9: Presuppositions of Quantified Sentences (or: *Every nation cherishes its king*)

**Read:** Heim (1983), *On the Projection Problem for Presuppositions*, §1.3, 3-4.

1. Why is *Every nation cherishes its king* a problem for Gazdar's theory?
2. Extra credit: Give another example of a sentence containing a part that has a presupposition containing a free variable (not involving possessives).
3. On p. 402, Heim suggests treating contexts as sets of pairs  $\langle g, w \rangle$ , where  $g$  is an assignment function (a sequence of individuals, or a function from integers to individuals) and  $w$  is a world.<sup>1</sup> For example, suppose:

$$c_1 = \left\{ \begin{array}{l} \langle \langle \text{Sweden, Sweden, Sweden} \rangle, w_1 \rangle \\ \langle \langle \text{Sweden, Sweden, Sweden} \rangle, w_2 \rangle \\ \langle \langle \text{Sweden, Sweden, Sweden} \rangle, w_3 \rangle \\ \langle \langle \text{Sweden, Sweden, America} \rangle, w_1 \rangle \\ \langle \langle \text{Sweden, Sweden, America} \rangle, w_2 \rangle \\ \langle \langle \text{Sweden, Sweden, America} \rangle, w_3 \rangle \\ \langle \langle \text{America, Sweden, America} \rangle, w_1 \rangle \\ \langle \langle \text{America, Sweden, America} \rangle, w_2 \rangle \\ \langle \langle \text{America, Sweden, America} \rangle, w_3 \rangle \\ \langle \langle \text{America, Sweden, Sweden} \rangle, w_1 \rangle \\ \langle \langle \text{America, Sweden, Sweden} \rangle, w_2 \rangle \\ \langle \langle \text{America, Sweden, Sweden} \rangle, w_3 \rangle \end{array} \right\}$$

And assume the following distribution of facts in worlds (which we can refer to as a 'model'):

- Sweden is a nation:  $\{w_1, w_2, w_3\}$
- America is a nation:  $\{w_1, w_2, w_3\}$
- Sweden has a king:  $\{w_1, w_2, w_3\}$
- America has a king:  $\{w_3\}$
- Sweden cherishes its king:  $\{w_1, w_3\}$
- America cherishes its king:  $\{w_3\}$

With this way of representing contexts, we can update contexts with sentences containing free variables. Updating a context  $c$  with (9) ' $x_i$  has a king' gives:  $c_1 \cup \{\langle g, w \rangle : g(i) \text{ has a king in } w\}$ . Let  $c_2 = 'c_1 + 'x_3 \text{ has a king}'$ . What sequence-world pairs does  $c_2$  contain?

4. The CCP that Heim gives for *every* is in (21), repeated here:

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<sup>1</sup>I will represent assignment functions as ordered sequences like  $\langle \text{America, Sweden, America} \rangle$  but also use function notation, so if  $g = \langle \text{America, Sweden, America} \rangle$  then  $g(1) = \text{America}$ ,  $g(2) = \text{Sweden}$ ,  $g(3) = \text{America}$ .

$c + \text{Every } x_i \text{ A, B} = \{\langle g, w \rangle \in c : \text{for every } a, \text{ if } \langle g^{i/a}, w \rangle \in c + \text{A}, \text{ then } \langle g^{i/a}, w \rangle \in c + \text{A} + \text{B}\}$

where:

- $g^{i/a}$  is the assignment that is the same as  $g$  except that the individual  $a$  is assigned to the number  $i$ , and
- $x_i$  must be a “new” variable in the sense of Heim’s (22):  $x_i$  is a **new variable** with respect to context  $c$  iff: For any two sequences  $g$  and  $g'$  that differ at most in their  $i$ -th member, and for any world  $w$ :  $\langle g, w \rangle \in c$  iff  $\langle g', w \rangle \in c$ .<sup>2</sup>

Let us consider an example to see how this works. Suppose that  $A = x_3$  is a nation, and  $B = x_3$  cherishes  $x_3$ ’s king. We want to compute  $c + \text{‘Every } x_3, x_3 \text{ is a nation, } x_3 \text{ cherishes } x_3 \text{’s king’}$  for an appropriate  $c$ . Here is a guide:

- (a) Is  $x_3$  “new” in  $c_1$  in the sense made explicit in (22) assuming that the only two elements of the domain are Sweden and America? Explain.
- (b) Is  $c_1 + A$  defined? Why or why not? If so, what is it? (Remember that an update is defined if the context entails all of its presuppositions. You can assume that ‘ $x_3$  is a nation’ has no presuppositions.)
- (c) Is  $(c_1 + A) + B$  defined? Why or why not? If so, what is it? Remember that in order to admit (satisfy-the-presuppositions-of) ‘ $x_i$  cherishes  $x_i$ ’s king’, a context must entail ‘ $x_i$  has a king’. By this Heim means that “it has to be a context  $c$  such that, for every  $\langle g, w \rangle \in c$ ,  $g(i)$  has a king in  $w$ ’.”
- (d) Suppose that we change the model so that America has a king in  $w_1, w_2$  and  $w_3$ . Is  $(c_1 + A) + B$  defined? If so, what is it?
- (e) Is  $c_1 + \text{‘Every } x_3, x_3 \text{ is a nation, } x_3 \text{ cherishes } x_3 \text{’s king’}$  defined? If so, explain why and compute its value and show how you arrived at your answer. If not, why not?
- (f) If we change the model so that America has a king in every world, is  $c + \text{‘Every } x_3, x_3 \text{ is a nation, } x_3 \text{ cherishes } x_3 \text{’s king’}$  defined? If so, why? If not, why not?
- (g) Using the model where both Sweden and America have a king in every world, maintaining the assumption that Sweden cherishes its king in  $w_1$  and  $w_3$ , what is the resulting set of sequence-world pairs? I.e., what is the value of:

$$c_1 + \text{‘Every } x_3, x_3 \text{ is a nation, } x_3 \text{ cherishes } x_3 \text{’s king’?}$$

5. For any context  $c$ , it turns out that  $c + \text{‘Every } x_3, x_3 \text{ is a nation, } x_3 \text{ cherishes } x_3 \text{’s king’}$  is defined whenever the following is true:

For every  $\langle g, w \rangle \in c \cup \{\langle g, w \rangle : g(3) \text{ is a nation in } w, g(3) \text{ has a king in } w\}$ .

Combined with the fact that  $x_3$  is required to be a “new” variable, this means that *Every nation cherishes its king* is predicted by Heim’s system to presuppose that every nation has a king. Explain how this universal presupposition arises.

6. Extra credit: Heim’s system predicts that (25) (*A fat man was pushing his bicycle*) presupposes that every fat man has a bicycle. Explain how this prediction comes about in your own words.

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<sup>2</sup>In other words, for every pair  $\langle g, w \rangle$  that you have in the context, for every  $x$  distinct from  $g(i)$ , there has to be another pair  $\langle g', w \rangle$  where  $g'(i) = x$ . The value of  $i$  cannot be restricted to certain individuals.